

## PANCYCLICITY WHEN EACH CYCLE CONTAINS $k$ CHORDS

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### Abstract

For integers  $n \geq k \geq 2$ , let  $c(n, k)$  be the minimum number of chords that must be added to a cycle of length  $n$  so that the resulting graph has the property that for every  $l \in \{k, k + 1, \dots, n\}$ , there is a cycle of length  $l$  that contains exactly  $k$  of the added chords. Affif Chaouche, Rutherford, and Whitty introduced the function  $c(n, k)$ . They showed that for every integer  $k \geq 2$ ,  $c(n, k) \geq \Omega_k(n^{1/k})$  and they asked if  $n^{1/k}$  gives the correct order of magnitude of  $c(n, k)$  for  $k \geq 2$ . Our main theorem answers this question as we prove that for every integer  $k \geq 2$ , and for sufficiently large  $n$ ,  $c(n, k) \leq k \lceil n^{1/k} \rceil + k^2$ . This upper bound, together with the lower bound of Affif Chaouche *et al.*, shows that the order of magnitude of  $c(n, k)$  is  $n^{1/k}$ .

**Keywords:** pancyclicity, chords.

**2010 Mathematics Subject Classification:** 05D99, 11B75.

### REFERENCES

- [1] F. Affif Chaouche, C. Rutherford and R. Whitty, *Pancyclicity when each cycle must pass exactly  $k$  Hamilton cycle chords*, Discuss. Math. Graph Theory **35** (2015) 533–539.  
doi:10.7151/dmgt.1818
- [2] J.A. Bondy, *Pancyclic graphs I*, J. Combin. Theory Ser. B **11** (1971) 80–84.  
doi:10.1016/0095-8956(71)90016-5
- [3] H.J. Broersma, *A note on the minimum size of a vertex pancyclic graph*, Discrete Math. **164** (1997) 29–32.  
doi:10.1016/S0012-365X(96)00040-4
- [4] J.C. George, A. Khodkar and W.D. Wallis, *Pancyclic and Bipancyclic Graphs*, 1st Ed. (Springer Briefs in Mathematics, Springer, 2016).

- [5] S. Griffin, *Minimal pancyclicity*.  
arXiv: 1312.0274v1 1 Dec 2013.
- [6] D.B. West, *Introduction to Graph Theory*, 2nd Edition (Pearson Education, Inc., 2001).

Received 26 September 2016

Revised 11 December 2017

Accepted 11 December 2017