SUM-LIST COLOURING OF UNIONS OF A HYPERCYCLE AND A PATH WITH AT MOST TWO VERTICES IN COMMON

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Abstract

Given a hypergraph $\mathcal{H}$ and a function $f : V(\mathcal{H}) \to \mathbb{N}$, we say that $\mathcal{H}$ is $f$-choosable if there is a proper vertex colouring $\phi$ of $\mathcal{H}$ such that $\phi(v) \in L(v)$ for all $v \in V(\mathcal{H})$, where $L : V(\mathcal{H}) \to 2^\mathbb{N}$ is any assignment of $f(v)$ colours to a vertex $v$. The sum choice number $\chi_{sc}(\mathcal{H})$ of $\mathcal{H}$ is defined to be the minimum of $\sum_{v \in V(\mathcal{H})} f(v)$ over all functions $f$ such that $\mathcal{H}$ is $f$-choosable. For an arbitrary hypergraph $\mathcal{H}$ the inequality $\chi_{sc}(\mathcal{H}) \leq |V(\mathcal{H})| + |E(\mathcal{H})|$ holds, and hypergraphs that attain this upper bound are called $sc$-greedy. In this paper we characterize $sc$-greedy hypergraphs that are unions of a hypercycle and a hyperpath having at most two vertices in common. Consequently, we characterize the hypergraphs of this type that are forbidden for the class of $sc$-greedy hypergraphs.

Keywords: hypergraphs, sum-list colouring, induced hereditary classes, forbidden hypergraphs.

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