

**CORRIGENDUM TO: BOUNDS ON THE NUMBER OF  
EDGES OF EDGE-MINIMAL, EDGE-MAXIMAL AND  
 $l$ -HYPERTREES [DISCUSSIONES MATHEMATICAE  
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**Abstract**

In this corrigendum, we correct the proof of Theorem 10 from our paper titled „Bounds on the number of edges of edge-minimal, edge-maximal and  $l$ -hypertrees”.

**Keywords:** hypertree, chain in hypergraph, edge-minimal hypertree, edge-maximal hypertree, 2-hypertree, Steiner system.

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1. THE CORRECTED PROOF OF THEOREM 10

In the original proof of Theorem 10, we stated that

$$\begin{aligned} & \frac{1}{k-1} \binom{n}{k-1} - \frac{1}{(k-1)(n-k+1)} |\mathcal{E}| \\ & \leq \frac{1}{k-1} \binom{n}{k-1} - \frac{1}{(k-1)^2(n-k+1)} \binom{n}{k-1}. \end{aligned}$$

This can only be true if  $|\mathcal{E}| \geq \frac{1}{k-1} \binom{n}{k-1}$ , but in reality, the exact opposite is true, i.e.,  $|\mathcal{E}| \leq \frac{1}{k-1} \binom{n}{k-1}$  (see Theorem 9).

Below, we present the corrected proof of Theorem 10.

**Theorem 10.** *If  $\mathcal{H} = (V, \mathcal{E})$  is a  $k$ -uniform 2-hypertree, then  $|\mathcal{E}| \leq \frac{1}{k-1} \binom{n}{k-1} - \frac{1}{(k-1)^3} \binom{n}{k-2}$ .*

**Proof.** We use the simple fact that  $\sum_{i=1}^{n-k+1} C_i \geq \frac{1}{n-k+1} |\mathcal{E}|$ , which follows from  $|\mathcal{E}| = \sum_{i=1}^{n-k+1} iC_i \leq (n-k+1) \sum_{i=1}^{n-k+1} C_i$ .

Comparing it to the Star-equation (Theorem 9), we get

$$\begin{aligned} |\mathcal{E}| &\leq \frac{1}{k-1} \binom{n}{k-1} - \frac{1}{(k-1)(n-k+1)} |\mathcal{E}| - \frac{1}{k-1} l \\ &\leq \frac{1}{k-1} \binom{n}{k-1} - \frac{1}{(k-1)(n-k+1)} |\mathcal{E}|, \end{aligned}$$

which implies, that

$$\begin{aligned} |\mathcal{E}| &\leq \left( (k-1) + \frac{1}{(n-k+1)} \right)^{-1} \binom{n}{k-1} \\ &= \left( \frac{1}{k-1} - \frac{1}{(k-1)^2(n-k+1) + (k-1)} \right) \binom{n}{k-1} \\ &\leq \left( \frac{1}{k-1} - \frac{1}{(k-1)^2(n-k+2)} \right) \binom{n}{k-1} \\ &= \frac{1}{k-1} \binom{n}{k-1} - \frac{1}{(k-1)^3} \binom{n}{k-2}. \end{aligned}$$

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