ON INDEPENDENT $[1,2]$-SETS IN TREES

Sahar A. Aleid, José Cáceres

AND

María Luz Puertas

Department of Mathematics
University of Almería, Spain

e-mail: sahar.aleid@ual.es
jcaceres@ual.es
mpuertas@ual.es

Abstract

An $[1,k]$-set $S$ in a graph $G$ is a dominating set such that every vertex not in $S$ has at most $k$ neighbors in it. If the additional requirement that the set must be independent is added, the existence of such sets is not guaranteed in every graph. In this paper we solve some problems previously posed by other authors about independent $[1,2]$-sets. We provide a necessary condition for a graph to have an independent $[1,2]$-set, in terms of spanning trees, and we prove that this condition is also sufficient for cactus graphs. We follow the concept of excellent tree and characterize the family of trees such that any vertex belongs to some independent $[1,2]$-set. Finally, we describe a linear algorithm to decide whether a tree has an independent $[1,2]$-set. This algorithm can be easily modified to obtain the cardinality of a smallest independent $[1,2]$-set of a tree.

Keywords: domination, independence, spanning trees, excellent trees.

2010 Mathematics Subject Classification: 05C69.

References


$^1$Partially supported by Phoenix Project (Erasmus Mundus Programme), MTM2014-60127-P (Ministerio de Economía y Competitividad) and FQM305 (Junta de Andalucía).


Received 5 October 2016
Revised 23 December 2016
Accepted 23 January 2017