

## ON $H$ -IRREGULARITY STRENGTH OF GRAPHS

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### Abstract

New graph characteristic, the total  $H$ -irregularity strength of a graph, is introduced. Estimations on this parameter are obtained and for some families of graphs the precise values of this parameter are proved.

**Keywords:**  $H$ -covering,  $H$ -irregular labeling,  $H$ -irregularity strength.

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