

CYCLE DOUBLE COVERS OF INFINITE PLANAR GRAPHS

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Abstract

In this paper, we study the existence of cycle double covers for infinite planar graphs. We show that every infinite locally finite bridgeless k -indivisible graph with a 2-basis admits a cycle double cover.

Keywords: cycle double cover, infinite planar graph.

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