TWIN MINUS TOTAL DOMINATION NUMBERS IN DIRECTED GRAPHS

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Abstract

Let $D=(V,A)$ be a finite simple directed graph (shortly, digraph). A function $f: V \rightarrow \{-1,0,1\}$ is called a twin minus total dominating function (TMTDF) if $f(N^-(v)) \geq 1$ and $f(N^+(v)) \geq 1$ for each vertex $v \in V$. The twin minus total domination number of $D$ is $\gamma^*_{mt}(D) = \min \{w(f) \mid f$ is a TMTDF of $D\}$. In this paper, we initiate the study of twin minus total domination numbers in digraphs and we present some lower bounds for $\gamma^*_{mt}(D)$ in terms of the order, size and maximum and minimum in-degrees and out-degrees. In addition, we determine the twin minus total domination numbers of some classes of digraphs.

Keywords: twin minus total dominating function, twin minus total domination number, directed graph.

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References


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