

LARGE DEGREE VERTICES IN LONGEST CYCLES OF GRAPHS, I

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Abstract

In this paper, we consider the least integer d such that every longest cycle of a k -connected graph of order n (and of independent number α) contains all vertices of degree at least d .

Keywords: longest cycle, large degree vertices, order, connectivity, independent number.

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