THE DISTANCE MAGIC INDEX OF A GRAPH

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Abstract

Let $G$ be a graph of order $n$ and let $S$ be a set of positive integers with $|S| = n$. Then $G$ is said to be $S$-magic if there exists a bijection $\phi : V(G) \rightarrow S$ satisfying $\sum_{x \in N(u)} \phi(x) = k$ (a constant) for every $u \in V(G)$. Let $\alpha(S) = \max \{s : s \in S\}$. Let $i(G) = \min \alpha(S)$, where the minimum is taken over all sets $S$ for which the graph $G$ admits an $S$-magic labeling. Then $i(G) − n$ is called the distance magic index of the graph $G$. In this paper we determine the distance magic index of trees and complete bipartite graphs.

Keywords: distance magic labeling, distance magic index, $S$-magic graph, $S$-magic labeling.

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References

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