BIPARTITION POLYNOMIALS, THE ISING MODEL
AND DOMINATION IN GRAPHS

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Abstract

This paper introduces a trivariate graph polynomial that is a common
generalization of the domination polynomial, the Ising polynomial, the matching
polynomial, and the cut polynomial of a graph. This new graph polynomial, called the bipartition polynomial, permits a variety of interesting

1Research supported by ESF.

2Research supported by the Austrian National Research Network S11403-N23 (RiSE) of the
Austrian Science Fund (FWF), and by the Vienna Science and Technology Fund (WWTF) grant
PROSEED.
representations, for instance as a sum ranging over all spanning forests. As a consequence, the bipartition polynomial is a powerful tool for proving properties of other graph polynomials and graph invariants. We apply this approach to show that, analogously to the Tutte polynomial, the Ising polynomial introduced by Andrén and Markström in [3], can be represented as a sum over spanning forests.

**Keywords:** domination, Ising model, graph polynomial.

**2010 Mathematics Subject Classification:** 05C30, 05C31, 05C69.

**References**


Received 23 January 2014
Revised 16 September 2014
Accepted 16 September 2014