

## ON RADIO CONNECTION NUMBER OF GRAPHS

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### Abstract

Given a graph  $G$  and a vertex coloring  $c$ ,  $G$  is called  $l$ -radio connected if between any two distinct vertices  $u$  and  $v$  there is a path such that coloring  $c$  restricted to that path is an  $l$ -radio coloring. The smallest number of colors needed to make  $G$   $l$ -radio connected is called the  $l$ -radio connection number of  $G$ . In this paper we introduce these notions and initiate the study of connectivity through radio colored paths, providing results on the 2-radio connection number, also called  $L(2, 1)$ -connection number: lower and upper bounds, existence problems, exact values for known classes of graphs and graph operations.

**Keywords:** radio connection number, radio coloring,  $L(2, 1)$ -connection number,  $L(2, 1)$ -connectivity,  $L(2, 1)$ -labeling.

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