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Note

ALMOST SELF-COMPLEMENTARY UNIFORM HYPERGRAPHS [1]

Adam Paweł Wojda

AGH University of Science and Technology
Faculty of Applied Mathematics
Al. Mickiewicza 30, 30-059 Kraków, Poland

e-mail: wojda@uci.agh.edu.pl

Abstract

A k-uniform hypergraph (k-hypergraph) is *almost self-complementary* if it is isomorphic with its complement in the complete k-uniform hypergraph minus one edge. We prove that an almost self-complementary k-hypergraph of order n exists if and only if $\binom{n}{k}$ is odd.

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