

ON H -IRREGULARITY STRENGTH OF GRAPHS

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Abstract

New graph characteristic, the total H -irregularity strength of a graph, is introduced. Estimations on this parameter are obtained and for some families of graphs the precise values of this parameter are proved.

Keywords: H -covering, H -irregular labeling, H -irregularity strength.

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