

## CYCLE DOUBLE COVERS OF INFINITE PLANAR GRAPHS

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### Abstract

In this paper, we study the existence of cycle double covers for infinite planar graphs. We show that every infinite locally finite bridgeless  $k$ -indivisible graph with a 2-basis admits a cycle double cover.

**Keywords:** cycle double cover, infinite planar graph.

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