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SOME TOUGHNESS RESULTS IN INDEPENDENT DOMINATION CRITICAL GRAPHS

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Abstract

A subset S of V(G) is an independent dominating set of G if S is independent and each vertex of G is either in S or adjacent to some vertex of S. Let i(G) denote the minimum cardinality of an independent dominating set of G. A graph G is k-i-critical if i(G) = k, but i(G + uv) < k for any pair of non-adjacent vertices u and v of G. In this paper, we establish that if G is a connected 3-i-critical graph and S is a vertex cutset of G with $|S| \ge 3$, then $\omega(G-S) \le \frac{1+\sqrt{8|S|+1}}{2}$, improving a result proved by Ao [3], where $\omega(G-S)$ denotes the number of components of G-S. We also provide a characterization of the connected 3-i-critical graphs G attaining the maximum number of $\omega(G-S)$ when S is a minimum cutset of size 2 or 3.

Keywords: domination critical, toughness.

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