

EIGENVALUE CONDITIONS FOR INDUCED SUBGRAPHS

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Abstract

Necessary conditions for an undirected graph G to contain a graph H as induced subgraph involving the smallest ordinary or the largest normalized Laplacian eigenvalue of G are presented.

Keywords: induced subgraph, eigenvalue.

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